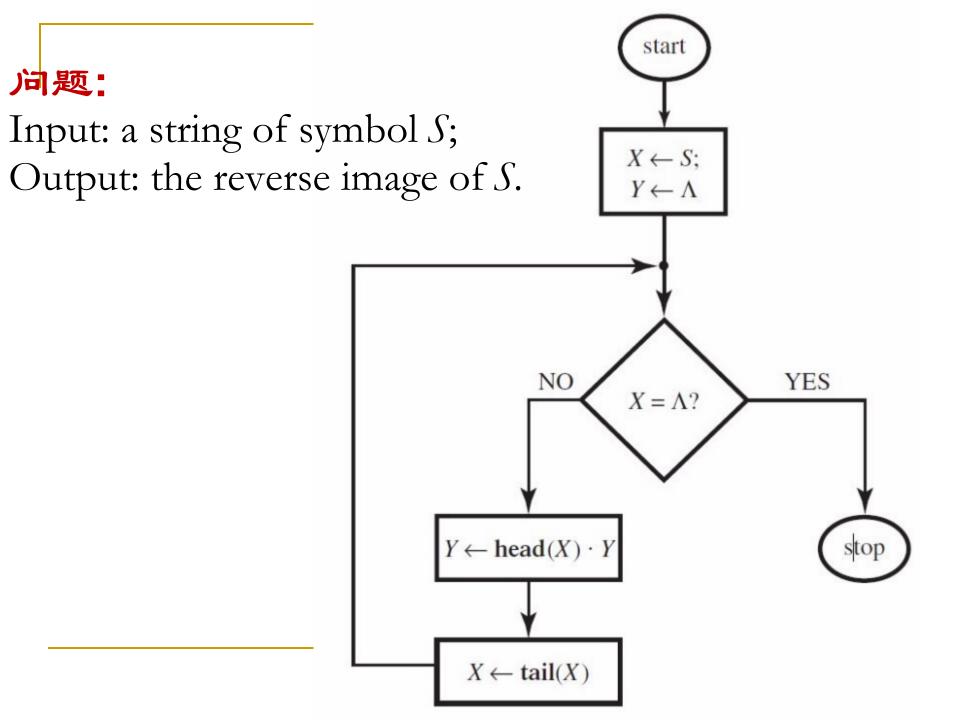


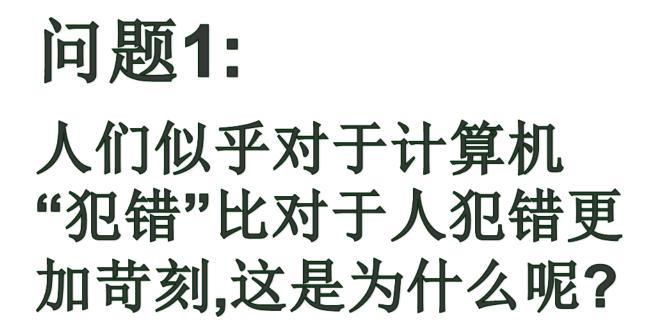
2014年2月25日

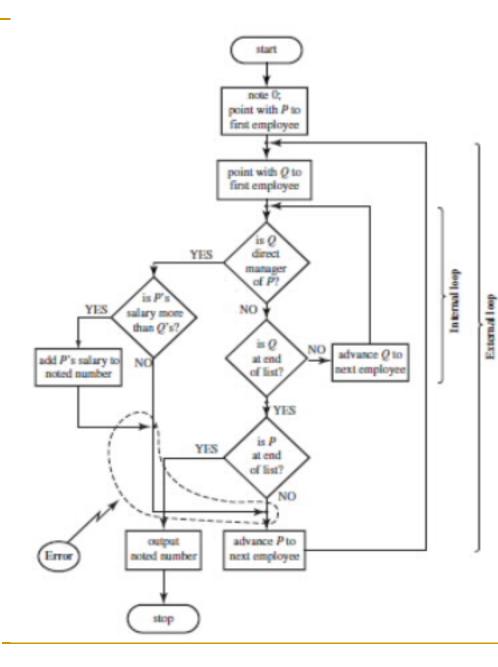
As discussed in Chapter 1, an algorithmic problem can be concisely divided into two parts:

- 1. a specification of the set of legal inputs; and
- 2. the relationship between the inputs and the desired outputs.

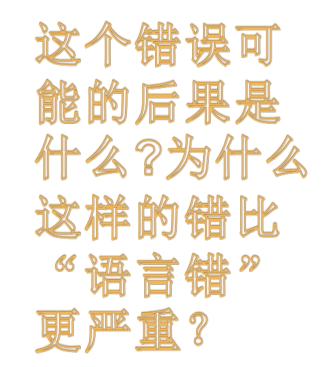
这段话和我们今天的主题什么关系?













书上的对文本中出现"money" 一词的句子计数的例子出现了什 么样的错误,你能说出它的性质 与前一个例子有什么不同吗?

几种不同的错误

- ■"语言错"
 - □ 很容易被语言处理软件发现,甚至自动纠正。
- ■"语义错"
 - □ 合格的程序员很少会犯这类错误。
- ■解题逻辑错误
 - □"粗心"造成的错误。

■ 常见(相对来说) **不常见,但这个是真的"伤脑筋"!** ■ "真正的"逻辑错误。



"Computers Do Not Err!" 你如何理解这句话?

Test and debugging

- A designer might try out an algorithm on several typical and atypical inputs and not find the error. In fact, a programmer will normally test a program on numerous inputs, sometimes called test sets, and will gradually rid it of its language errors and most of its logical errors.
- Most algorithmic problems have infinite sets of legal inputs, and hence infinitely many candidate test sets, each of which has the potential of exposing a new error.

Debugging 的局限性

Logical errors, someone once said, are like mermaids. The mere fact that you haven't seen one doesn't mean they don't exist.

. As someone

once put it, testing and debugging cannot be used to demonstrate the absence of errors in software, only their presence.

"someone" believed to be Dijkstra:

Program testing can be used to show the presence of bugs, but never to show their absence!

Also, Dijkstra believed to say:

Programming is one of the most difficult branches of applied mathematics; the poorer mathematicians had the better remain pure mathematicians.

关于debugging的思考

■为什么我们可以:

The process of repeatedly executing an algorithm, or running a program, with the intention of finding and eliminating errors is called debugging?

Infinite computation

为什么infinite computation 有时也被称为 infinite loop?

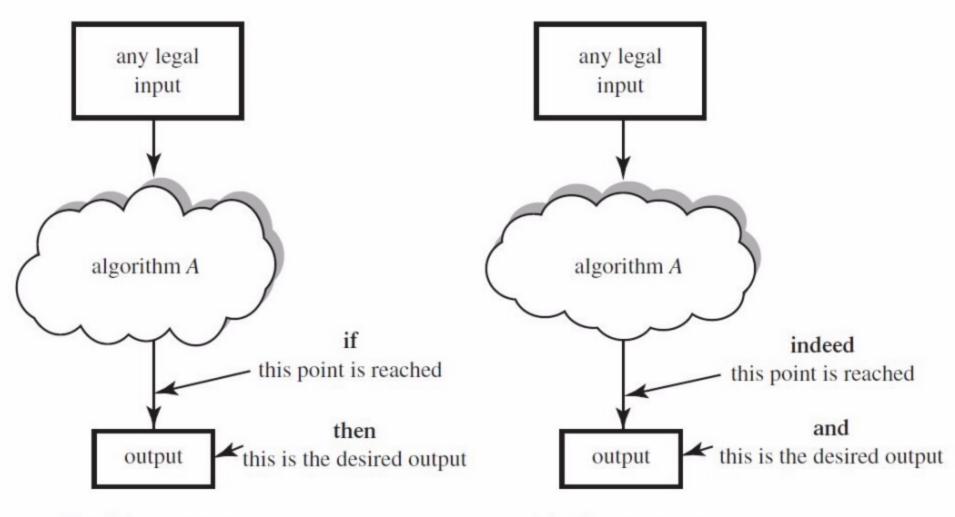
Infinite loop有什么作用?

如何避免不正确的Infinite loop出现?

As discussed in Chapter 1, an algorithmic problem can be concisely divided into two parts:

- 1. a specification of the set of legal inputs; and
- 2. the relationship between the inputs and the desired outputs.

部分和完全正确性



Partial correctness

Total correctness

"部分"与"完全"正确性

Euclid algorithm

- □ input: nonnegative integer *m*,*n*
- output: gcd(m,n)
- procedure

Euclid(int m,n)

if *n*=0

if *d* is the GCD of *m* and *n*, it must be theGCD of *n* and (*m* mod *n*)

then return m

else return Euclid(*n*, *m* mod *n*)

问题5:

(*m* mod *n*) is always less than *n*, so, the algorithm must terminate

你能否用这个例子解释 Partial 和 Total正确性?

算法正确性证明:

■ 自动验证:

 some sort of super-algorithm that would accept as inputs a description of an algorithmic problem *P* and an algorithm *A* that is proposed as a solution, and would determine if indeed *A* solves *P*.

■ 人工证明:

Can we ourselves prove our algorithms to be correct? Is there any way in which we can use formal, mathematical techniques to realize this objective?

如何利用什么数学技术来证明算法的正确性? "部分正确性":

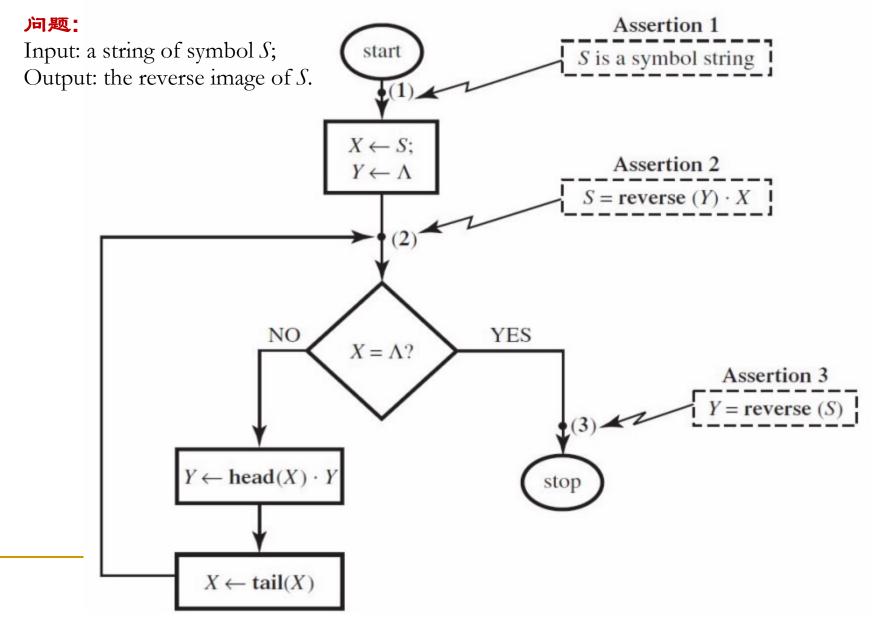
- We do not care whether execution ever reaches the endpoint, but that if it does we will not be in a situation where the outputs differ from the expected ones.
- we wish to capture the behavior of the algorithm by making careful statements about what it is doing at certain points.

we thus attach intermediate assertions to various checkpoints in the algorithm's text.

如何理解以下文字?

Attaching an assertion to a checkpoint means that we believe that whenever execution reaches the point in question, in any execution of the algorithm on any legal input, the assertion will be true.

Intermediate Assertions at Checkpoints



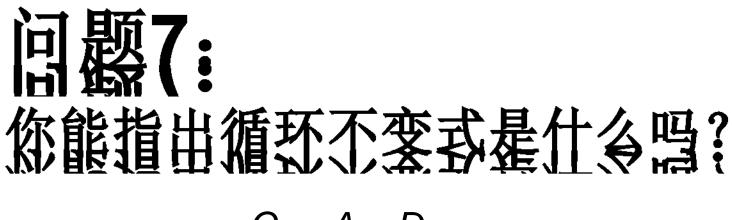


这些intermediate assertions 为什么被称为"invariants"?

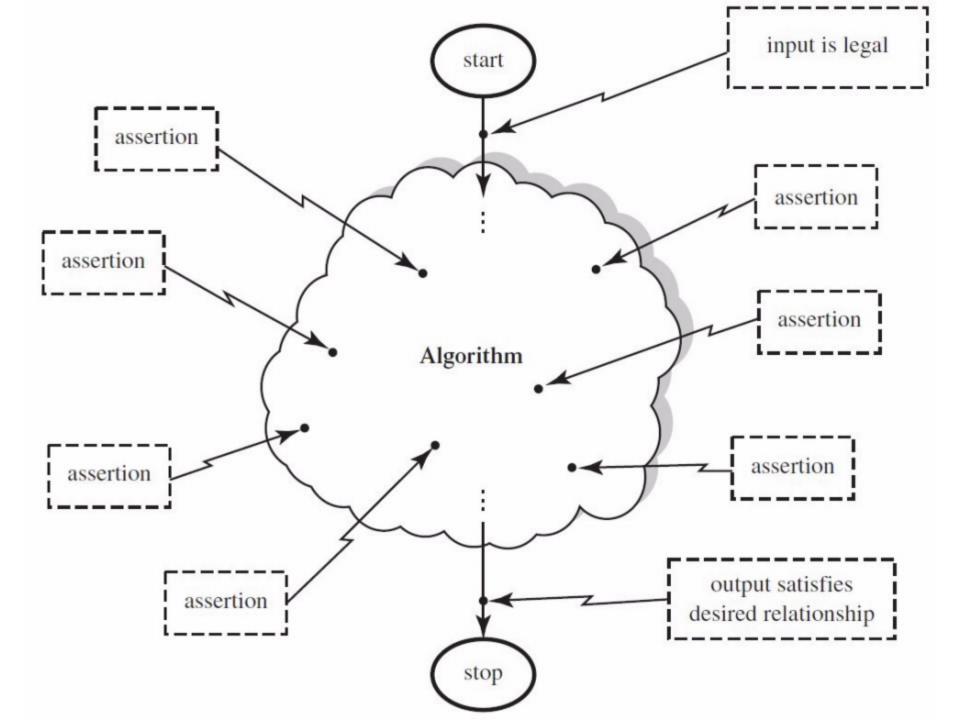
subroutine square of A:

(1) set C to 0;
(2) set D to 0;
(3) while (D A) do set C to C+A; set D to D+1;
(4) return C.

这个过程计算A的平方。



 $C_k = A \quad D_k$



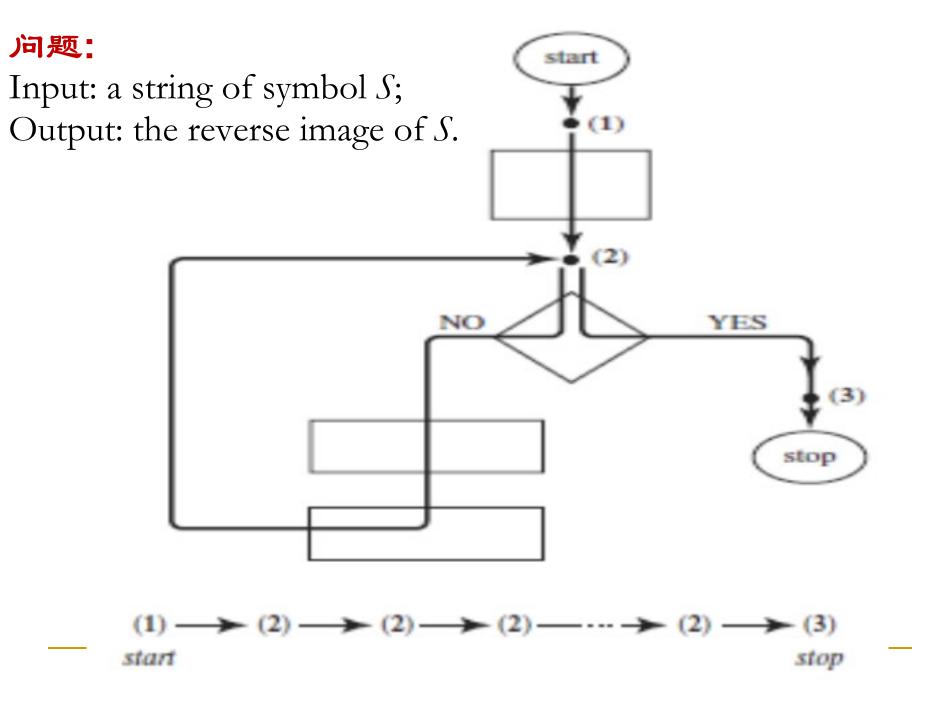
Then:

■ 要证明一个算法的部分正确性:

□ 在哪里设置checkpoint?

□ 什么样的"局部特性"用断言形式描述?

 proceeding locally from checkpoint to checkpoint does not bring about any violations of the invariance properties



我们可以/必须证明:

 $(1 \rightarrow 2)$: for any string *S*, after carrying out the two instructions $X \leftarrow S$; $Y \leftarrow \Lambda$, the equality $S = \mathbf{reverse}(Y) \cdot X$ will hold.

 $(2 \rightarrow 3)$: if $S = reverse(Y) \cdot X$, and $X = \Lambda$, then Y = reverse(S).

 $(2 \rightarrow 2)$: if $S = \mathbf{reverse}(Y) \cdot X$, and $X \neq \Lambda$, then after carrying out the instructions $Y \leftarrow \mathbf{head}(X) \cdot Y$; $X \leftarrow \mathbf{tail}(X)$, the same equality, namely $S = \mathbf{reverse}(Y) \cdot X$, will hold for the new values of X and Y.

 $(2 \rightarrow 2)$: if $S = reverse(Y) \cdot X$, and $X \neq \Lambda$, then $S = reverse(head(X) \cdot Y) \cdot tail(X)$.

收敛性: total正确性的证明方法

- showing that something good eventually happens (not that bad things do not); namely, that the algorithm indeed reaches its endpoint and terminates successfully.
- find some quantity and show that it converges:
 - quantity keeps decreasing as execution proceeds from one checkpoint to another, but that it cannot decrease forever: there is some bound below which it can never go



The convergent is simply the length of the string *X*.