

## 第 7 讲: 离散概率基础

姓名: \_ 学号: \_

评分: \_\_\_\_\_ 评阅: \_\_\_\_\_

2022 年 3 月 30 日

请独立完成作业, 不得抄袭。  
若得到他人帮助, 请致谢。  
若参考了其它资料, 请给出引用。  
鼓励讨论, 但需独立书写解题过程。

### 1 作业 (必做部分)

题目 1 (CS 5.1-10)

解答:

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题目 2 (CS 5.1-12)

解答:

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题目 3 (CS 5.2-4)

解答:

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题目 4 (CS 5.2-10)

解答:

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题目 5 (CS 5.3-2)

解答:

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题目 6 (CS 5.3-12)

解答:

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题目 7 (CS 5.4-10)

解答:

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题目 8 (CS 5.4-15)

解答:

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## 2 作业 (选做部分)

题目 1 (The Ballot Problem)

In an election, candidate  $A$  receives  $n$  votes, and candidate  $B$  receives  $m$  votes where  $n > m$ . Assuming that all orderings are equally likely, what is the probability that  $A$  is always ahead in the count of votes?

解答:

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## 3 Open Topics

Open Topics 1 (Monty Hall Problem)

请介绍 Monty Hall Problem, 尽量讲清楚各种版本背后的概率解释。

参考资料:

- [Monty Hall problem @ wiki](#)
- [“21” Movie @ Youtube](#)

**Open Topics 2 (Shuffling Cards)**

请参考下列资料介绍“洗牌”中的数学。(不必追求严格推导, 主要介绍基本思想。)

“How often does one have to shuffle a deck of cards until it is random?”

参考资料:

- Section “Top-in-at-random shuffles” of Chapter 30 of Book: “Proofs from THE BOOK” (见课程网站)

## 4 反馈