问题与反馈

2014.12.24

• Degrees 3, 4,4,4,5,6,6.

- Show that there exists
- (a) a 4-regular planar graph and a 4-regular nonplanar graph
- (b) a 5-regular planar graph and a 5regular nonplanar graph
- (c) no r-regular planar graph for r >= 6.

- Give an example of each of the following or explain why no such example exists.
- (a) a planar graph of order 4
- (b) a nonplanar graph of order 4
- (c) a nonplanar graph of order 6 that contains neither K5 nor K3,3 as a subgraph.
- (d) a plane graph having 5 vertices, 10 edges, and 7 regions.
- (e) a planar graph of order n>=3 and size m with m =3n6.
- (f) a nonplanar graph of order n>=3 and size m with m =3n-6.

• Whether the graph K4 \times K2 is planar.

- The chromatic number of
- (a) the Petersen graph; (b) the n-cube Qn,
- (c) the wheel Wn \sim = Cn + K1.

• Chromatic number of a tree

- Prove or disprove
- (a) If a planar graph contains a triangle, then its chromatic number is 3.
- (b) if there is a 4-colorable of a graph G, then X(G) =4.
- (c) if it can be shown that there is no a 3coloring of a graph G, then X(G) = 4.
- (d) if G is a graph with X(G)<=4, then G is planar.

• Prove that every graph of order 6 with chromatic number 3 has at most 12 edges.

